

**Dualidade Onda-Partícula**  
**e**  
**Princípio da Incerteza**

# Breve cronologia dos modelos para a luz

- Isaac Newton (1640 - 1725): sucesso do modelo mecânico para explicar vários fenômenos.



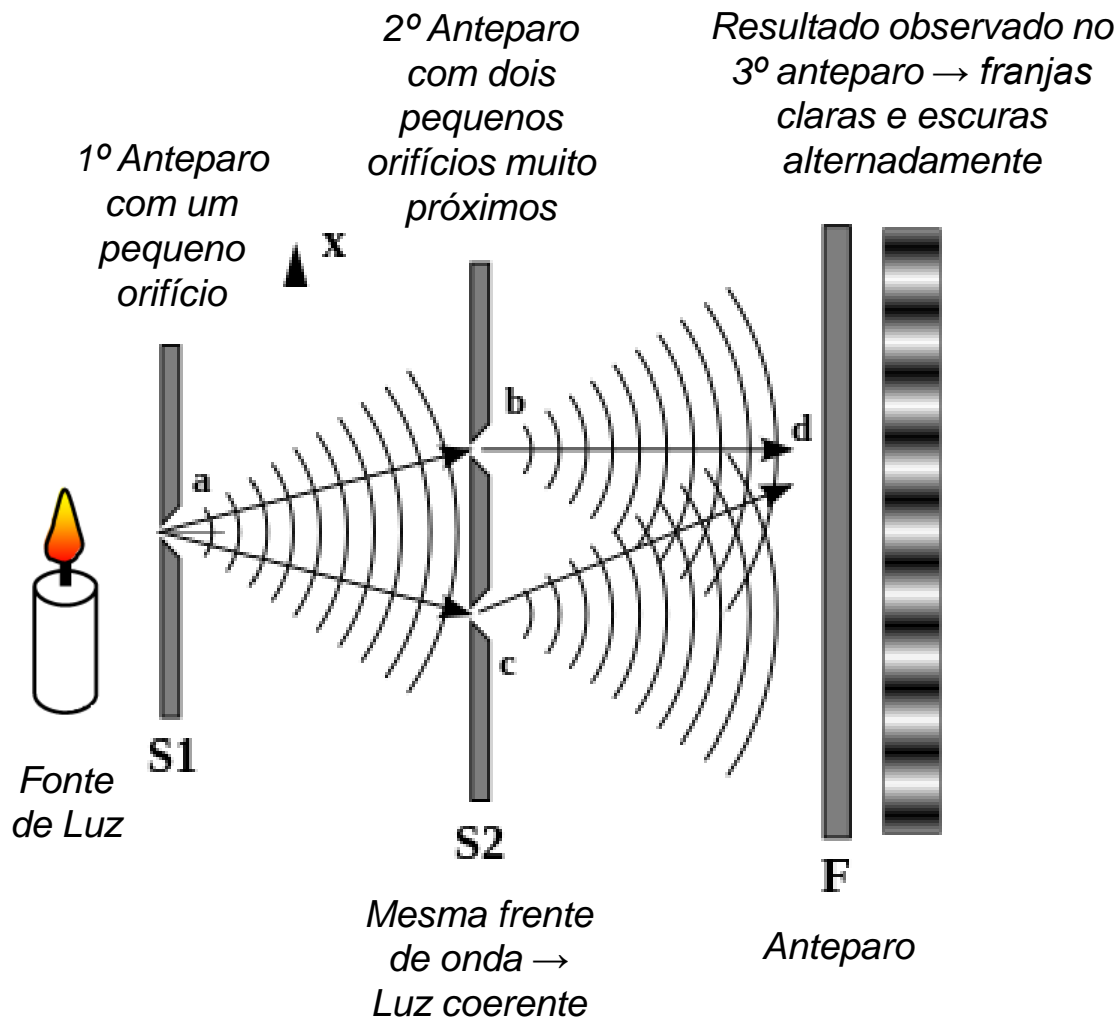
## Modelo Corpuscular da Luz

- Christian Huygens (1629 - 1695): fenômenos luminosos poderiam ser explicados mais facilmente considerando-os como ondas.

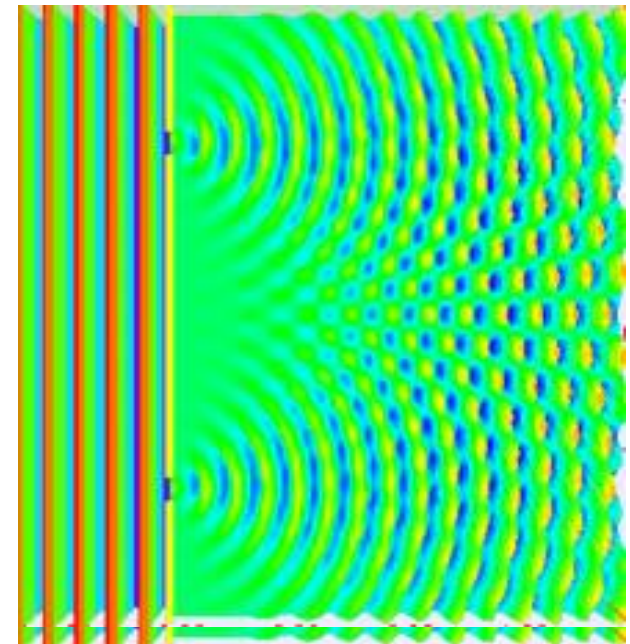


## Modelo Ondulatório da Luz

# Cronologia - Experimento da dupla fenda



Thomas Young  
1773 - 1829

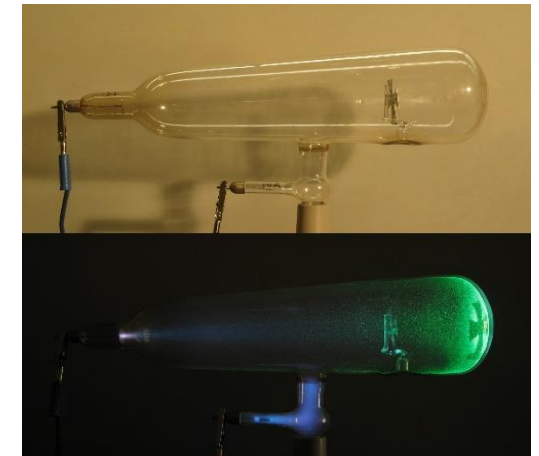
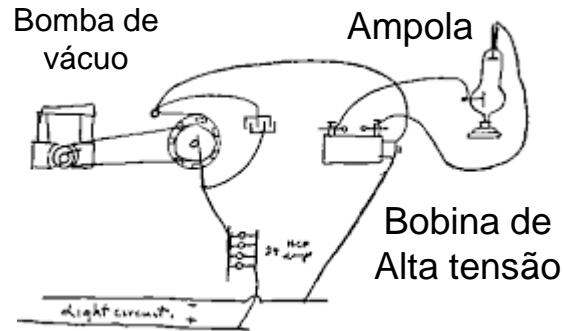
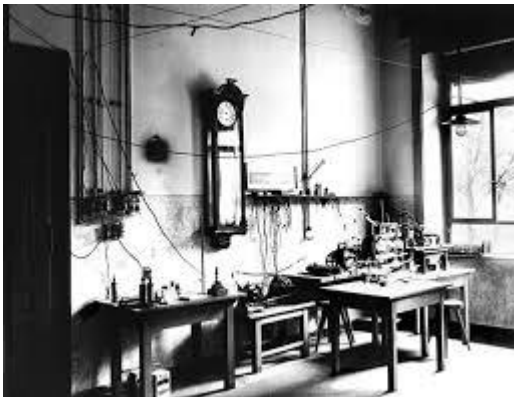


Natureza Ondulatória da Luz  
(1.801)

# Cronologia - Descoberta dos Raios X - 08/11/1895



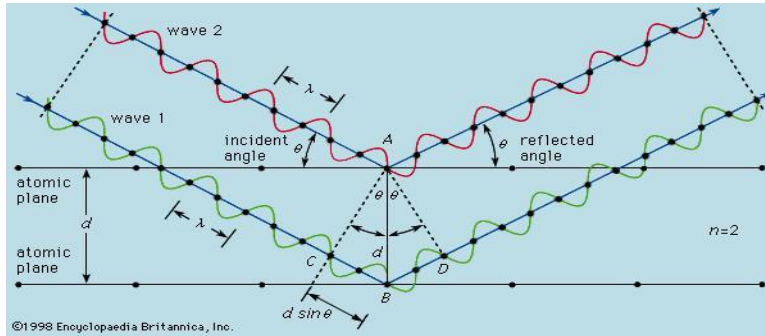
Wilhelm W. Roentgen  
1845 - 1923  
Nobel de **1.901**



# Cronologia

## Cristalografia de Raios X

1912 - 1913

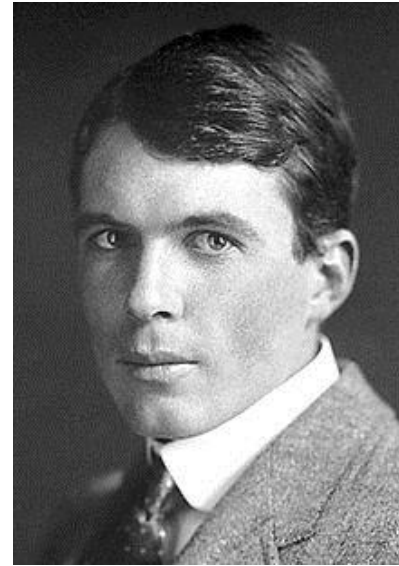


- *Análise da estrutura de cristais*
- *Parâmetros de rede cristalina*
- *Composição química*

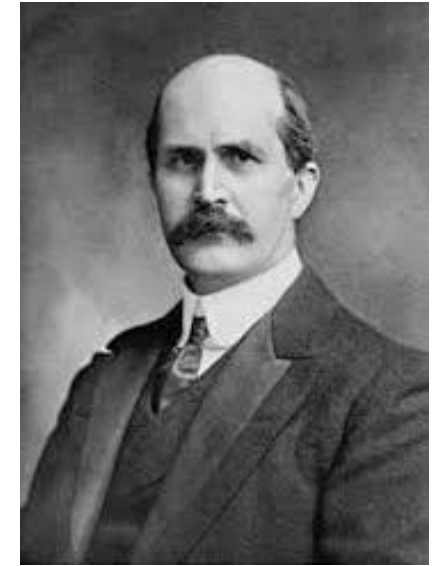
$$n \cdot \lambda = 2 \cdot d \cdot \sin \theta$$

$n$  é inteiro positivo  
(Interferência Construtiva)

$$\begin{aligned} d &= 0,91 \times 10^{-10} \text{ m;} \\ n &= 1; \quad \theta = 65^\circ \\ \lambda &= 2 \times 0,91 \times 10^{-10} \times \sin 65^\circ = \\ &= 1,65 \text{ \AA} \end{aligned}$$

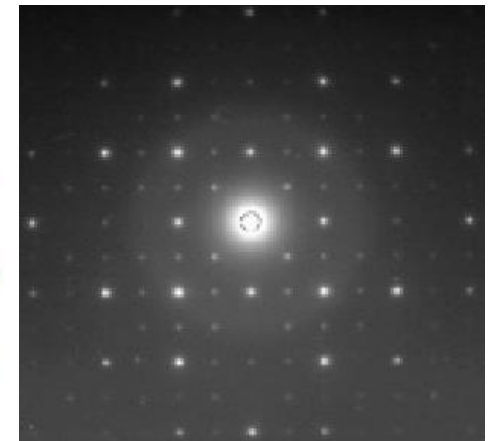
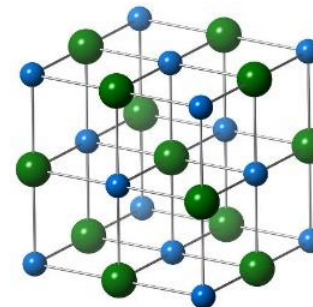


William L. Bragg  
1890 - 1971  
Nobel de **1.915**



Lawrence H. Bragg  
1862 - 1942  
Nobel de **1.915**

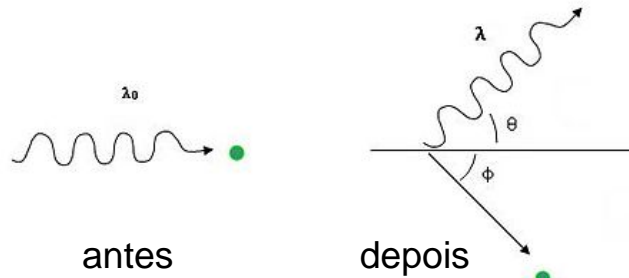
Padrão de difração  
de Raios X do NaCl





- em **1.916**, Einstein demonstra que os fótons possuem momento linear, uma característica de matéria em movimento.

$$p = \frac{hf}{c} = \frac{h}{\lambda}$$



Albert Einstein  
1879 - 1955  
Nobel de **1.921**

- em **1.924**, de Broglie anuncia que os elétrons apresentam características tanto ondulatórias como corpusculares, comportando-se de um ou outro modo, dependendo do experimento específico.

$$\lambda = \frac{h}{p}$$

$$f = \frac{E}{h}$$

Relações de **de Broglie**

$$\lambda = \frac{h}{p} = \frac{6,62 \times 10^{-34}}{9,11 \times 10^{-31} \times 4,4 \times 10^6} = 1,65 \text{ \AA}$$

$$\phi_{\text{átomo}} \approx 10^{-10} \text{ m}$$

$$\phi_{\text{núcleo}} \approx 10^{-14} \text{ m}$$



Louis V.P.R. de Broglie  
1892 - 1987  
Nobel de **1.929**

# Comprovação Experimental



Joseph John Thomson  
1856 - 1940  
Nobel de **1.906**



George Paget Thomson  
1892 - 1975  
Nobel de **1.937**



Clinton J. Davisson  
1881 - 1958  
Nobel de **1.937**

Lester H. Germer  
1896 - 1971

JOSEPH J. THOMSON

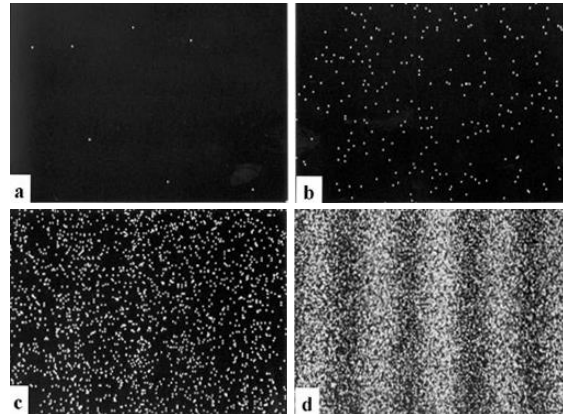
Carriers of negative electricity

*Nobel Lecture, December 11, 1906*

*Introductory*

In this lecture I wish to give an account of some investigations which have led to the conclusion that the carriers of negative electricity are bodies, which I have called corpuscles, having a mass very much smaller than that of the atom of any known element, and are of the same character from whatever source the negative electricity may be derived.

The first place in which corpuscles were detected was a highly exhausted tube through which an electric discharge was passing. When an electric discharge is sent through a highly exhausted tube, the sides of the tube glow with a vivid green phosphorescence. That this is due to something proceeding in straight lines from the cathode - the electrode where the negative electricity enters the tube - can be shown in the following way (the experiment is one made many years ago by Sir William Crookes): A Maltese cross made of thin mica is placed between the cathode and the walls of the tube. When the discharge is past, the green phosphorescence no longer extends all over the end of the tube, as it did when the cross was absent.



*Second Series*

*December, 1927*

*Vol. 30, No. 6*

## THE PHYSICAL REVIEW

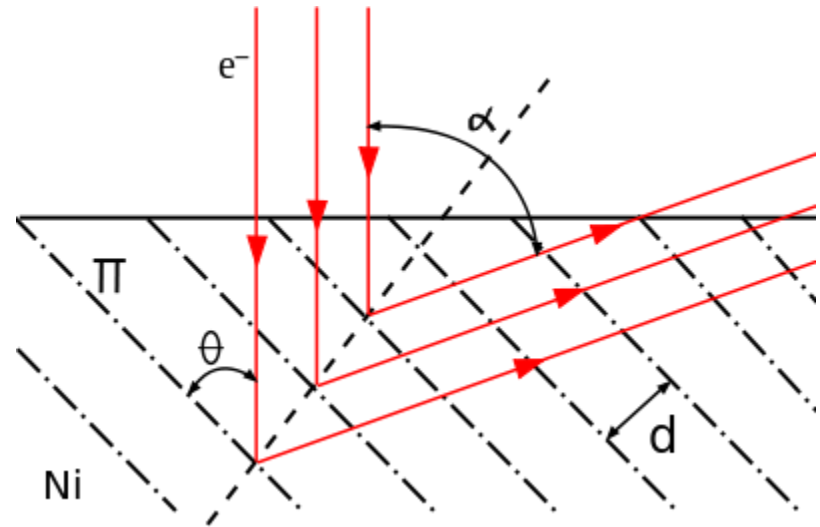
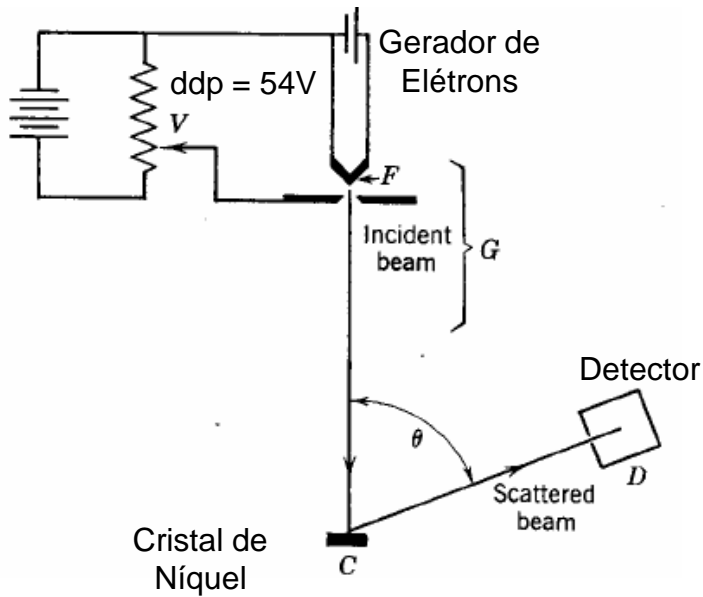
DIFFRACTION OF ELECTRONS BY A CRYSTAL OF NICKEL

BY C. DAVISSON AND L. H. GERMER

ABSTRACT

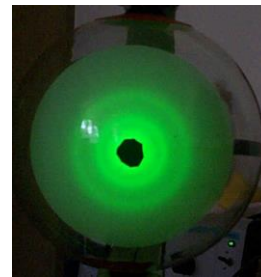
*The intensity of scattering of a homogeneous beam of electrons of adjustable speed incident upon a single crystal of nickel has been measured as a function of direction. The crystal is cut parallel to a set of its {111}-planes and bombardment is at normal incidence. The distribution in latitude and azimuth has been determined for such scattered electrons as have lost little or none of their incident energy.*

# Dispositivo Experimental



$$n \cdot \lambda = 2 \cdot d \cdot \text{sen } \theta$$

$n$  é inteiro positivo



Difração de Elétrons  
Tel 2555

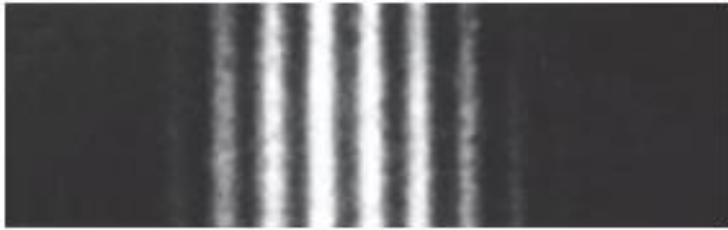
$$d = 0,91 \times 10^{-10} \text{ m};$$

$$n = 1; \quad \theta = 65^\circ$$

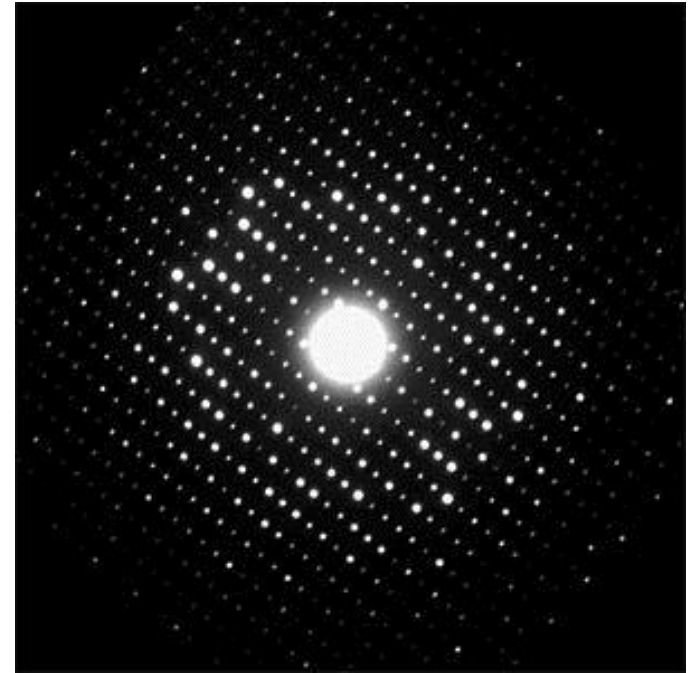
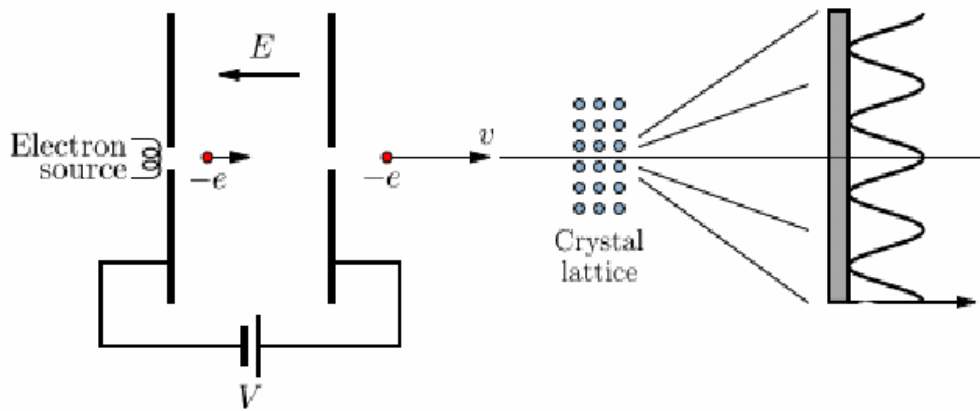
$$\lambda = 2 \times 0,91 \times 10^{-10} \times \sin 65^\circ = 1,65 \text{ \AA}$$



# Comprovação Experimental



C. H. Jönsson  
1960



Padrão de difração de elétrons em um cristal de *óxido de tântalo inorgânico*

## Exercícios

- 1) Determine o comprimento de onda de **de Broglie** para o caso de uma bola de futebol com massa de 445g, chutada com uma velocidade de 85 km/h.  $h = 6,626 \times 10^{-34} \text{ J}\cdot\text{s}$
- 2) Determine o comprimento de onda de **de Broglie** para o caso de um elétron, massa de  $9,11 \times 10^{-31} \text{ kg}$ , submetido a uma ddp de 100V (calcule  $v$ ).

# Princípio da Incerteza

$$\Delta x \cdot \Delta p \geq \frac{h}{4 \cdot \pi}$$

*“A posição e o momento linear de uma partícula não podem ser medidos simultaneamente, com uma precisão arbitrariamente alta.”*

3) Você está jogando futebol em um universo (muito diferente do nosso!) no qual a constante de Planck é 0,60 J.s. Qual é a indeterminação da posição de uma bola de 0,50 Kg que foi chutada com uma velocidade de 20 m/s se a indeterminação da velocidade é 1,0 m/s?

Dados:

$$h = 0,60 \text{ J} \cdot \text{s}$$

$$m_b = 0,50 \text{ Kg}$$

$$v_x = 20 \text{ m/s}$$

$$\Delta v_x = 1 \text{ m/s}$$

$$\Delta x = ?$$



Werner K. Heisenberg  
1901 - 1976  
Nobel de **1.932**

# **Referências Sitioográficas**

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<https://www.hitachi.com/rd/research/materials/quantum/index.html>

# **Comprovação Experimental**

- Estermann, Stern e Frisch

Todas as partículas materiais apresentam comportamento ondulatório;  
difração de feixes moleculares de H e He numa superfície de LiF